

Lect. 17: Two-Integrator-Loop Biquad (S&S 12.7)

One circuit configuration for several different second-order filters?

→ Two-integrator-loop biquad (biquad)

Consider
$$\frac{V_{\text{hp}}}{V_i} = \frac{Ks^2}{s^2 + s(\omega_0/Q) + \omega_0^2}$$

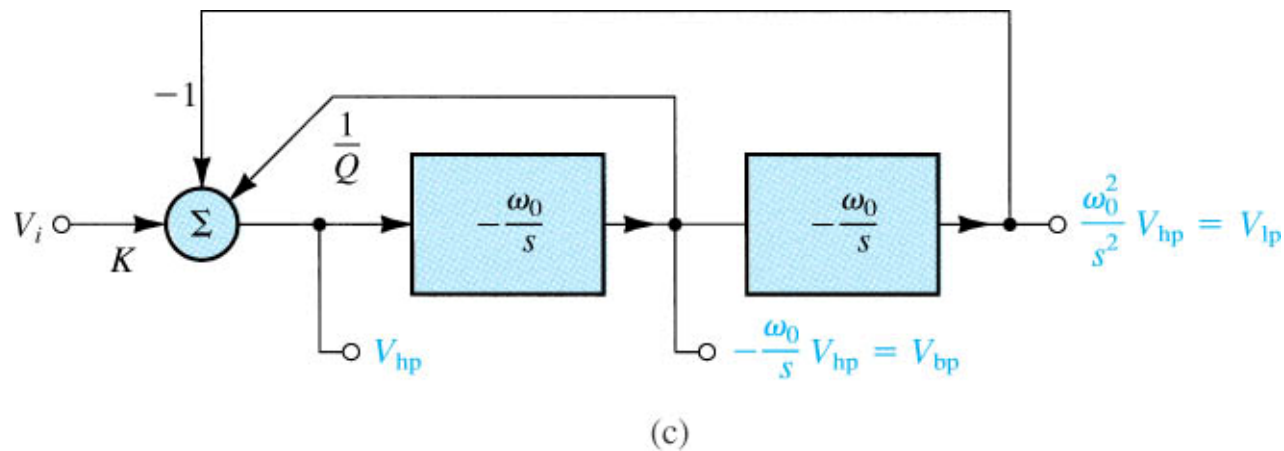
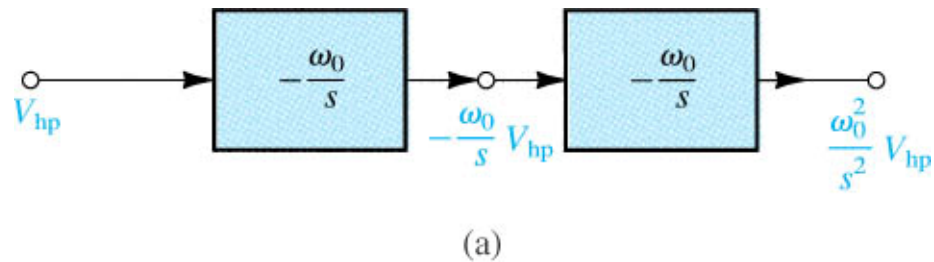
$$V_{\text{hp}} + \frac{1}{Q} \left(\frac{\omega_0}{s} V_{\text{hp}} \right) + \left(\frac{\omega_0^2}{s^2} V_{\text{hp}} \right) = KV_i$$

$$V_{\text{hp}} = KV_i - \frac{1}{Q} \frac{\omega_0}{s} V_{\text{hp}} - \frac{\omega_0^2}{s^2} V_{\text{hp}}$$

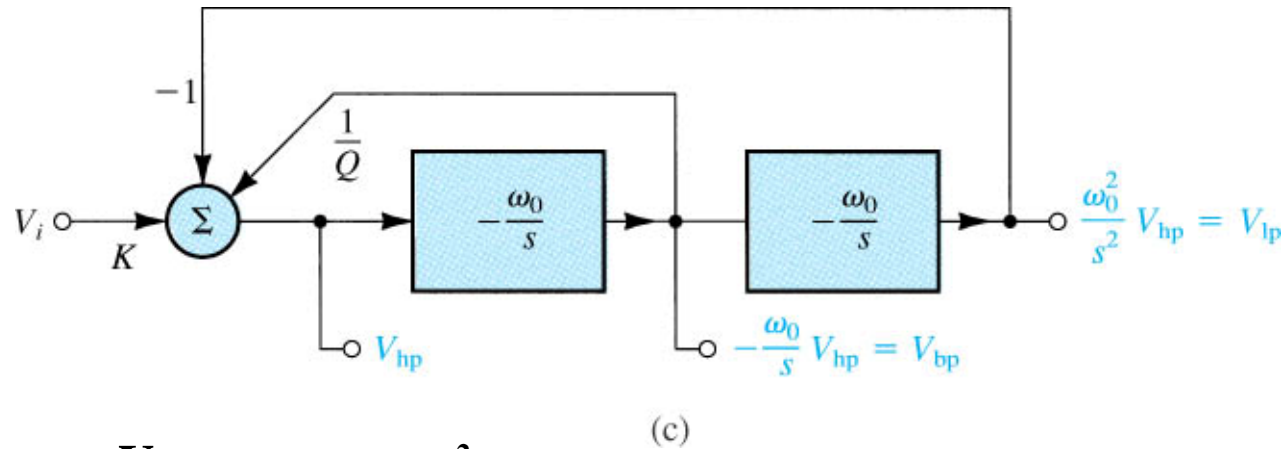
Lect. 17: Two-Integrator-Loop Biquad

$$V_{hp} = KV_i - \frac{1}{Q} \frac{\omega_0}{s} V_{hp} - \frac{\omega_0^2}{s^2} V_{hp}$$

Express the above equation graphically → block diagram



Lect. 17: Two-Integrator-Loop Biquad



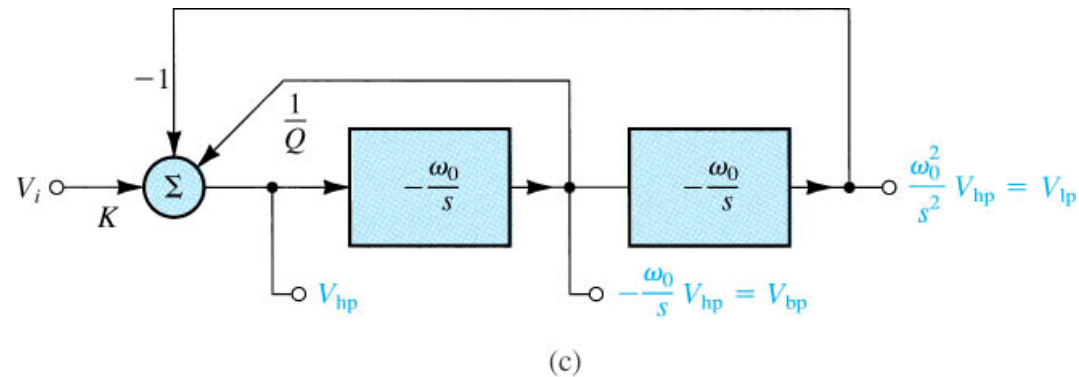
Since
$$\frac{V_{hp}}{V_i} = \frac{Ks^2}{s^2 + s(\omega_0/Q) + \omega_0^2},$$

$$\left(-\omega_0/s\right) \frac{V_{hp}}{V_i} = -\frac{K\omega_0 s}{s^2 + s(\omega_0/Q) + \omega_0^2} \quad \text{BP}$$

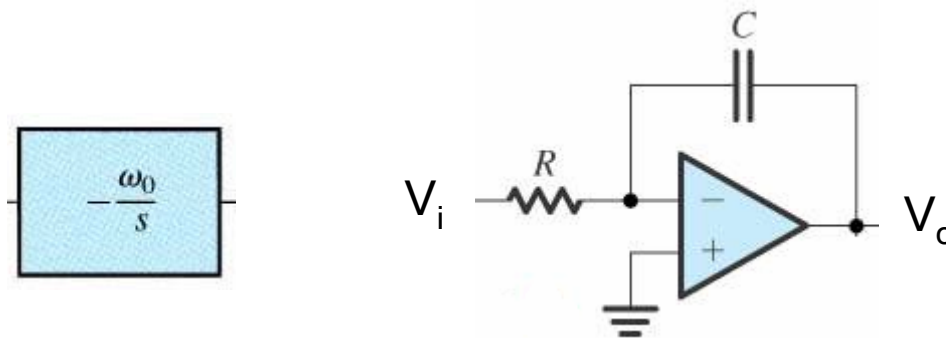
$$\left(\omega_0^2/s^2\right) \frac{V_{hp}}{V_i} = \frac{K\omega_0^2}{s^2 + s(\omega_0/Q) + \omega_0^2} \quad \text{LP}$$

Biquad → Universal Active Filter

Lect. 16: Two-Integrator-Loop Biquad



How to implement biquad?

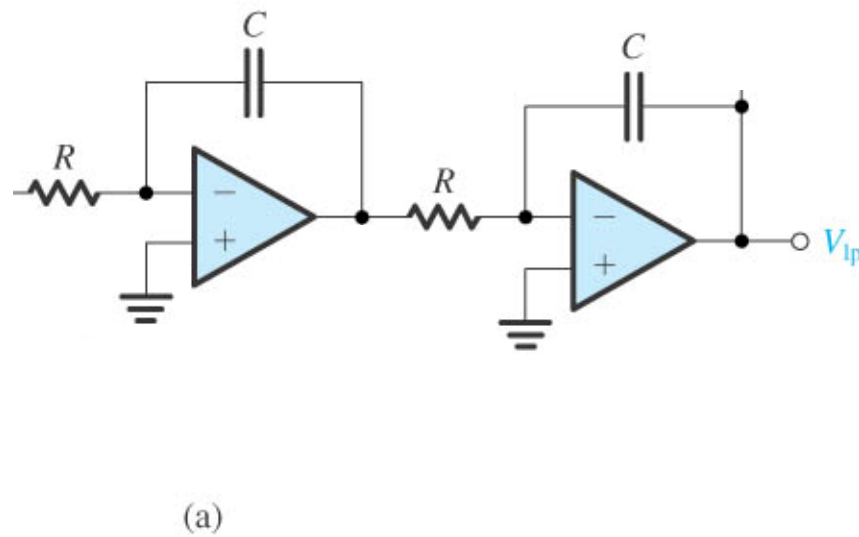
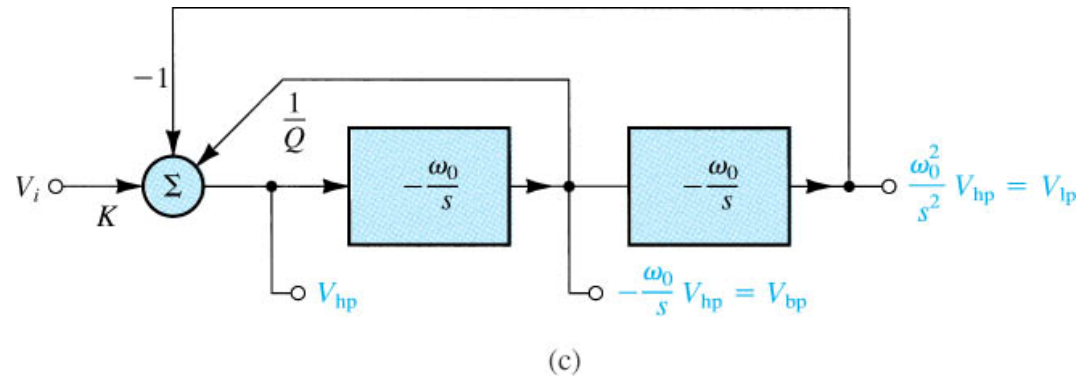


$$V_o = -\frac{V_i}{R} \cdot \frac{1}{sC}$$

$$\frac{V_o}{V_i} = -\frac{1}{RCs} = -\frac{\omega_0}{s}$$

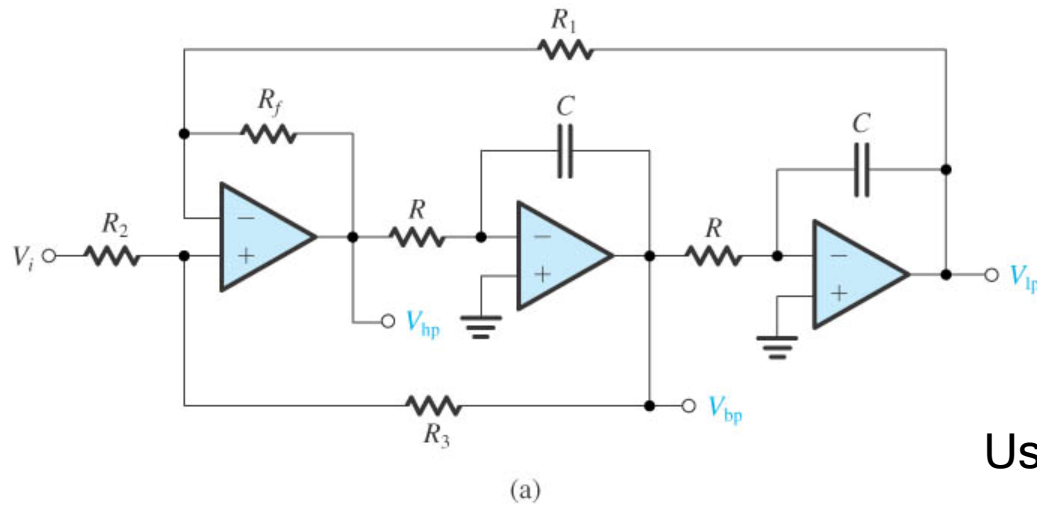
$$\omega_0 = \frac{1}{RC}$$

Lect. 17: Two-Integrator-Loop Biquad



Lect. 17: Two-Integrator-Loop Biquad

Kerwin-Huelsman-Newcomb (KHN) biquad

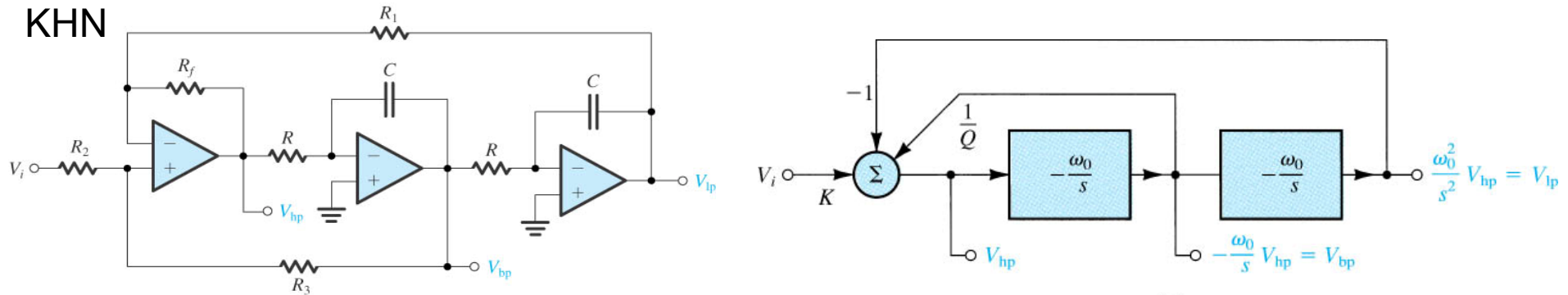


Use superposition (V_i , V_{bp} , V_{lp})

$$V_{hp} = \frac{R_3}{R_2 + R_3} \left(\frac{R_1 + R_f}{R_1} \right) V_i + \frac{R_2}{R_2 + R_3} \left(1 + \frac{R_f}{R_1} \right) V_{bp} - \frac{R_f}{R_1} V_{lp}$$

→ Weighted sum of V_i , V_{bp} , V_{lp}

Lect. 17: Two-Integrator-Loop Biquad



$$V_{hp} = \frac{R_3}{R_2 + R_3} \left(\frac{R_1 + R_f}{R_1} \right) V_i + \frac{R_2}{R_2 + R_3} \left(1 + \frac{R_f}{R_1} \right) V_{bp} - \frac{R_f}{R_1} V_{lp} \quad V_{hp} = KV_i - \frac{1}{Q} \frac{\omega_0}{s} V_{hp} - \frac{\omega_0^2}{s^2} V_{hp}$$

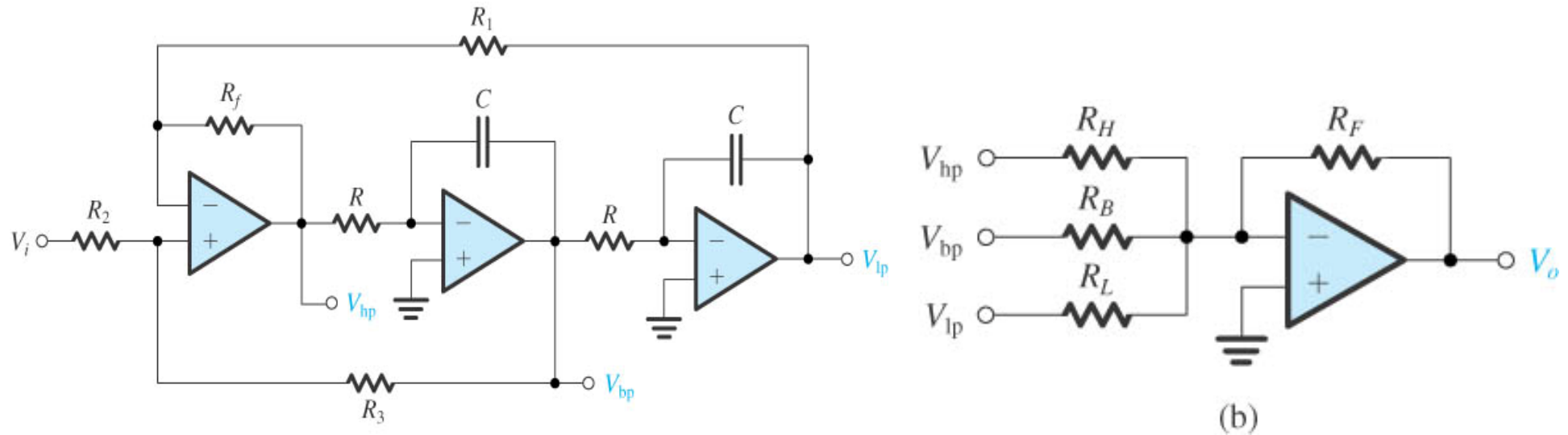
$$= \frac{R_3}{R_2 + R_3} \left(\frac{R_1 + R_f}{R_1} \right) V_i + \frac{R_2}{R_2 + R_3} \left(1 + \frac{R_f}{R_1} \right) \left(-\frac{\omega_0}{s} \right) V_{hp} - \frac{R_f}{R_1} \left(-\frac{\omega_0^2}{s^2} \right) V_{hp}$$

$$\therefore R_f/R_1 = 1 \quad \frac{2R_2}{R_2 + R_3} = \frac{1}{Q} \quad \therefore Q = \frac{R_2 + R_3}{2R_2} \quad K = \frac{2R_3}{R_2 + R_3} = 2 - \frac{1}{Q}$$

$$\omega_0 = ?$$

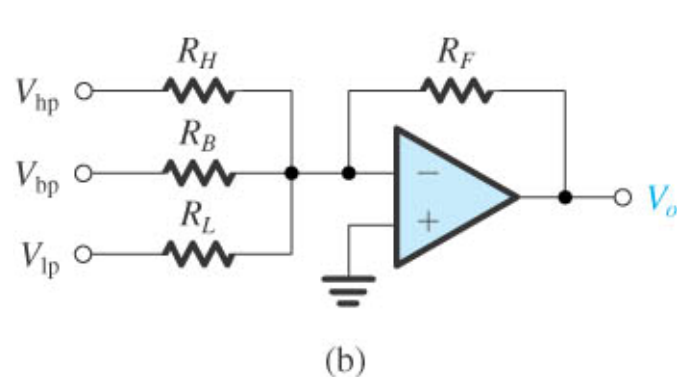
Lect. 17: Two-Integrator-Loop Biquad

How about Notch, All-Pass Filters?



Lect. 17: Two-Integrator-Loop Biquad

How about Notch, All-Pass Filters?



$$V_o = - \left(\frac{R_F}{R_H} V_{hp} + \frac{R_F}{R_B} V_{bp} + \frac{R_F}{R_L} V_{lp} \right)$$

$$V_{hp} = \frac{Ks^2}{s^2 + s(\omega_0/Q) + \omega_0^2} V_i$$

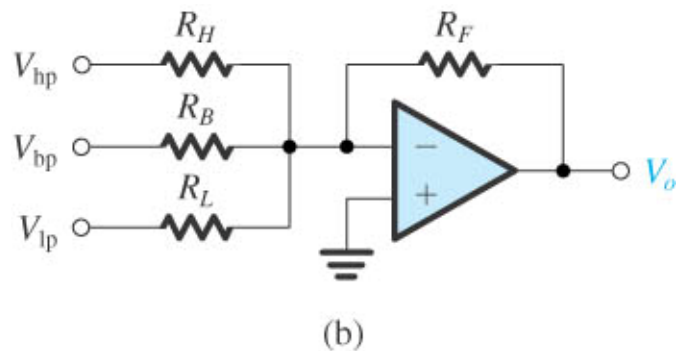
$$V_{bp} = \left(-\frac{\omega_0}{s}\right) V_{hp} = \frac{-K\omega_0 s}{s^2 + s(\omega_0/Q) + \omega_0^2} V_i$$

$$V_{lp} = \left(\frac{\omega_0^2}{s^2}\right) V_{hp} = \frac{K\omega_0^2}{s^2 + s(\omega_0/Q) + \omega_0^2} V_i$$

$$\frac{V_o}{V_i} = - \frac{(R_F / R_H) K s^2 - (R_F / R_B) K \omega_0 s + (R_F / R_L) K \omega_0^2}{s^2 + s(\omega_0 / Q) + \omega_0^2}$$

Lect. 17: Two-Integrator-Loop Biquad

How about Notch, All-Pass Filters?



$$\frac{V_o}{V_i} = -K \frac{(R_F / R_H)s^2 - (R_F / R_B)\omega_0 s + (R_F / R_L)\omega_0^2}{s^2 + s(\omega_0 / Q) + \omega_0^2}$$

Notch Filter: $T(s) = a_2 \frac{s^2 + \omega_0^2}{s^2 + s\frac{\omega_0}{Q} + \omega_0^2}$

$$\frac{R_F}{R_H} = 1, \quad R_B = \infty, \quad \frac{R_F}{R_L} = 1$$

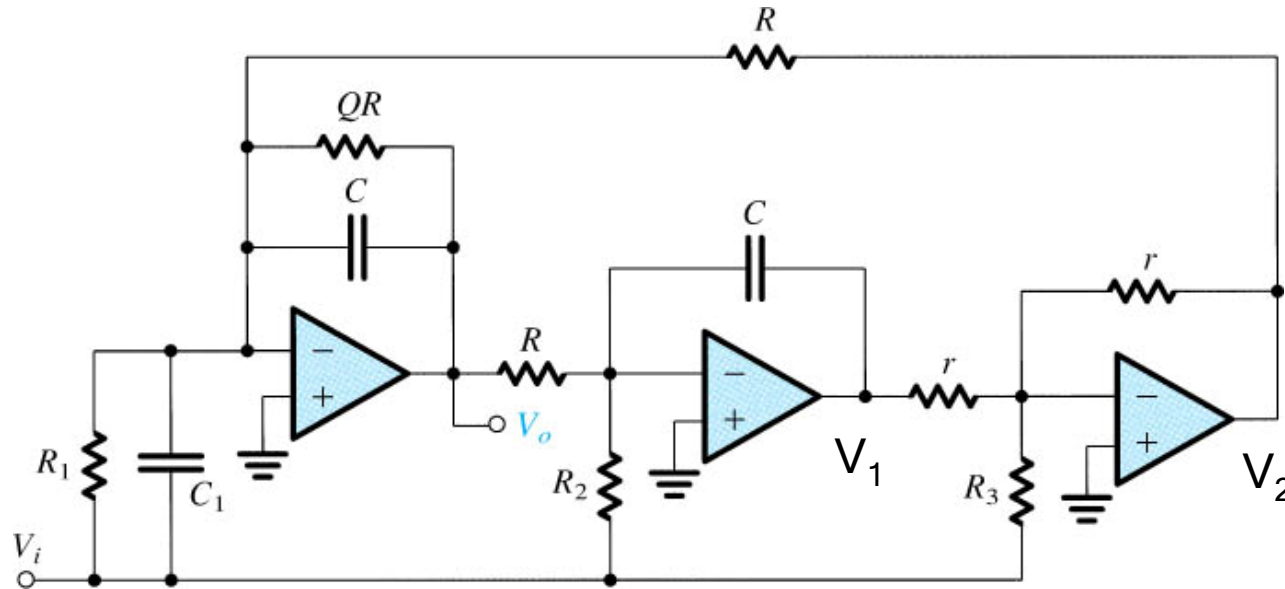
All-Pass Filter $T(s) = a_2 \frac{s^2 - s\frac{\omega_0}{Q} + \omega_0^2}{s^2 + s\frac{\omega_0}{Q} + \omega_0^2}$

$$\frac{R_F}{R_H} = 1, \quad \frac{R_F}{R_B} = \frac{1}{Q}, \quad \frac{R_F}{R_L} = 1$$

Lect. 17: Two-Integrator-Loop Biquad

Other types of biquads?

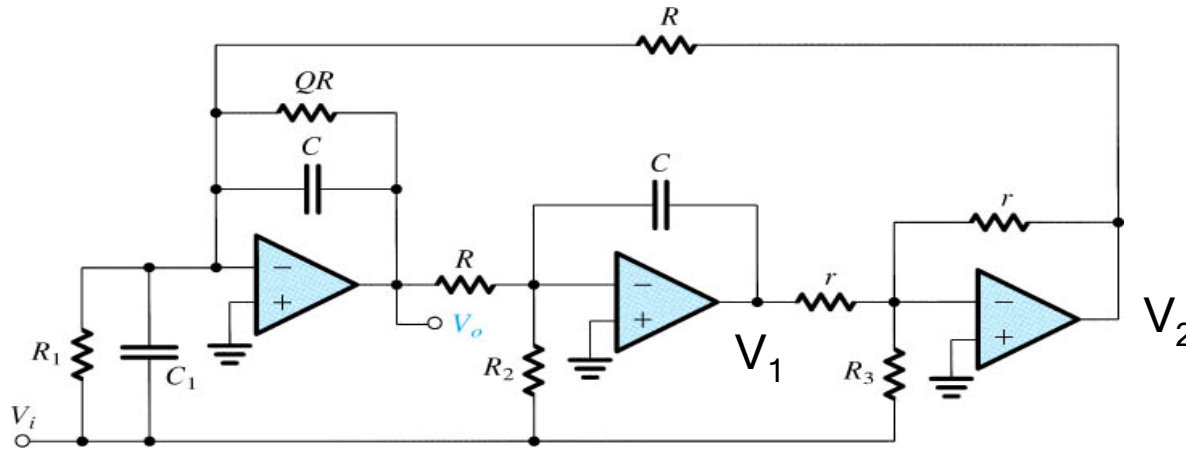
One type of Tow-Thomas biquad



$$V_o = - \left(\frac{V_i}{R_1 \parallel \frac{1}{sC_1}} + \frac{V_2}{R} \right) (QR \parallel \frac{1}{sC}) \quad V_2 = - \left(\frac{V_i}{R_3} + \frac{V_1}{r} \right) r \quad V_1 = - \left(\frac{V_o}{R} + \frac{V_i}{R_2} \right) \frac{1}{sC}$$

Lect. 17: Two-Integrator-Loop Biquad

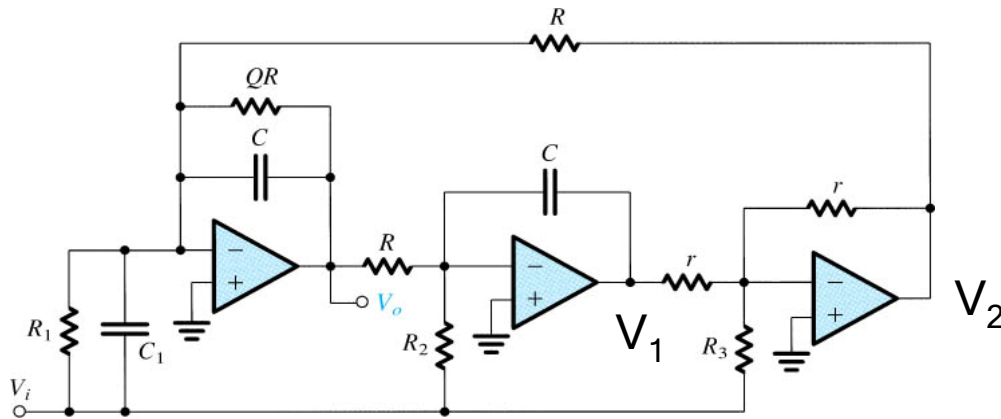
Tow-Thomas biquad



$$\frac{V_o}{V_i} = - \frac{s^2 \left(\frac{C_1}{C} \right) + s \frac{1}{C} \left(\frac{1}{R_1} - \frac{r}{RR_3} \right) + \frac{1}{C^2 RR_2}}{s^2 + s \frac{1}{QCR} + \frac{1}{C^2 R^2}}$$

$$\omega_0 = CR$$

Lect. 17: Two-Integrator-Loop Biquad



For LP $T(s) = \frac{a_0}{s^2 + s\frac{\omega_0}{Q} + \omega_0^2}$

$C_1 = 0 \quad R_1 = \infty, R_3 = \infty$

DC Gain: $\frac{R}{R_2}$

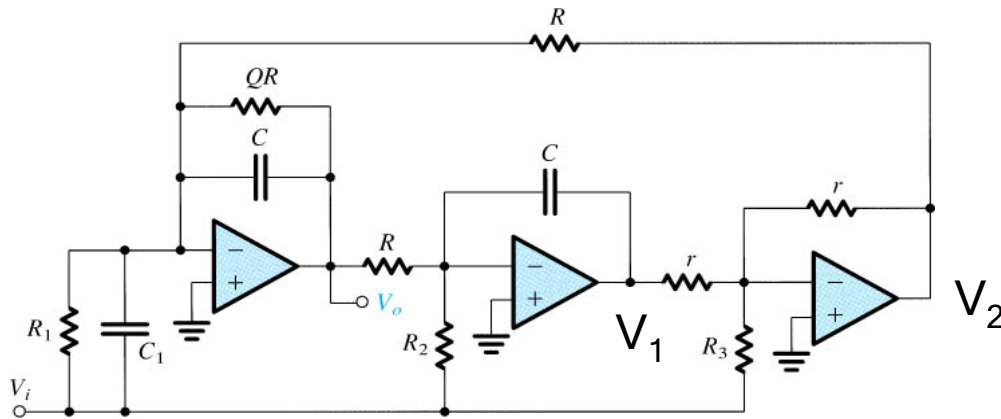
$$\frac{V_o}{V_i} = - \frac{s^2 \left(\frac{C_1}{C} \right) + s \frac{1}{C} \left(\frac{1}{R_1} - \frac{r}{RR_3} \right) + \frac{1}{C^2 RR_2}}{s^2 + s \frac{1}{QCR} + \frac{1}{C^2 R^2}}$$

For HP $T(s) = \frac{a_2 s^2}{s^2 + s\frac{\omega_0}{Q} + \omega_0^2}$

$R_1 = \infty, R_2 = \infty, R_3 = \infty$

HF Gain: $\frac{C_1}{C_2}$

Lect. 17: Two-Integrator-Loop Biquad



For BP $T(s) = \frac{a_1 s}{s^2 + s \frac{\omega_0}{Q} + \omega_0^2}$

$C_1 = 0 \quad R_2 = \infty$

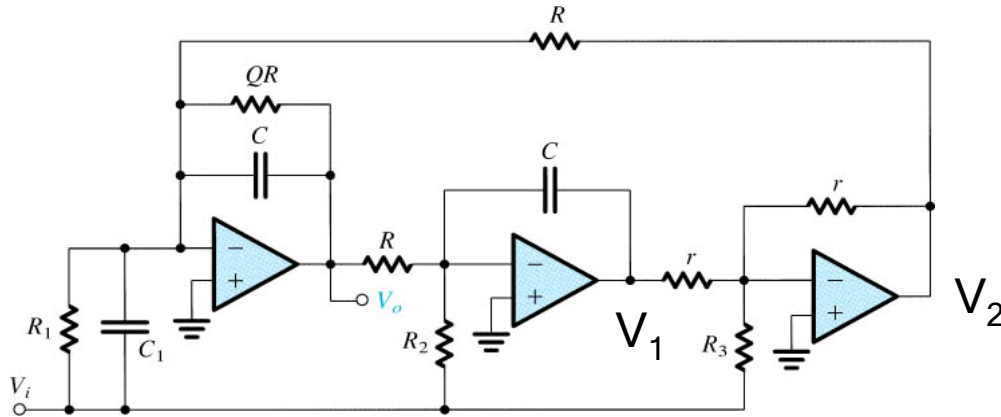
HF Gain: $\frac{C_1}{C_2}$

$$\frac{V_o}{V_i} = - \frac{s^2 \left(\frac{C_1}{C} \right) + s \frac{1}{C} \left(\frac{1}{R_1} - \frac{r}{RR_3} \right) + \frac{1}{C^2 RR_2}}{s^2 + s \frac{1}{QCR} + \frac{1}{C^2 R^2}}$$

For BR $T(s) = a_2 \frac{s^2 + \omega_0^2}{s^2 + s \frac{\omega_0}{Q} + \omega_0^2}$

$R_1 = \infty, R_3 = \infty$

Lect. 17: Two-Integrator-Loop Biquad



For AP

$$T(s) = a_2 \frac{s^2 - s \frac{\omega_0}{Q} + \omega_0^2}{s^2 + s \frac{\omega_0}{Q} + \omega_0^2}$$

(For the case of $a_2=1$)

$$\frac{V_o}{V_i} = - \frac{s^2 \left(\frac{C_1}{C} \right) + s \frac{1}{C} \left(\frac{1}{R_1} - \frac{r}{RR_3} \right) + \frac{1}{C^2 RR_2}}{s^2 + s \frac{1}{QCR} + \frac{1}{C^2 R^2}}$$

$$C_1 = C$$

$$R_1 = \infty \quad R_3 = Qr$$

$$R_2 = R$$